

Introduction to Reinforcement Learning

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Plan of the Lecture

1. Brief historical overview of reinforcement learning
2. A multi-disciplinary field
3. The agent-environment model

1 Reinforcement Learning: from Psychology to Machine Learning

1.1 Animal Learning, Experimental Psychology, and Neuroscience

The law of effect [Thorndike, 1911]:

“Of several responses made to the same situation, those which are accompanied or closely followed by **satisfaction** to the animal will, other things being equal, be more firmly connected with the situation, so that, when it recurs, they will be more likely to recur; those which are accompanied or closely followed by **discomfort** to the animal will, other things being equal, have their connections with that situation weakened, so that, when it recurs, they will be less likely to occur. The greater the satisfaction or discomfort, the greater the strengthening or weakening of the bond.”

Experimental psychology

- *Classical (human and) animal conditioning*: “the magnitude and timing of the conditioned response changes as a result of the contingency between the conditioned stimulus and the unconditioned stimulus” [Pavlov, 1927].
- *Operant conditioning (or instrumental conditioning)*: process by which humans and animals **learn** to behave in such a way as to obtain **rewards** and avoid **punishments** [Skinner, 1938].
- *Remark*: **reinforcement** denotes any form of conditioning, either positive (*rewards*) or negative (*punishments*).

Computational neuroscience

- *Hebbian learning*: development of formal models of how the synaptic weights between neurons are reinforced by simultaneous activation. “*Cells that fire together, wire together.*” [Hebb, 1961].

- *Emotions theory*: model on how the emotional process can bias the decision process [Damasio, 1994].
- *Dopamine and basal ganglia model*: direct link with motor control and decision-making (e.g., [Doya, 1999]).
- *Remark*: **reinforcement** denotes the effect of dopamine (and surprise).

1.2 Optimal Control Theory, Dynamic Programming, and Machine Learning

Optimal control theory and dynamic programming

- *Optimal control*: formal framework to define optimization methods to derive control policies in continuous time control problems [Pontryagin and Neustadt, 1962].
- *Dynamic programming*: set of methods used to solve control problems by decomposing them into subproblems so that the optimal solution to the global problem is the conjunction of the solutions to the subproblems [Bellman, 2003].
- *Remark*: **reinforcement** denotes an objective function to maximize (or minimize).

Reinforcement learning

- *Objective*: **learning** of a behavior strategy (a *policy*) which maximizes the long term sum of rewards (**delayed reward**) by a direct interaction (**trial-and-error**) with an unknown and uncertain (e.g., stochastic) environment.
- *Examples*: sensorimotor learning, autonomous robotics, portfolio management, games (e.g., backgammon, chess, go), web advertising.

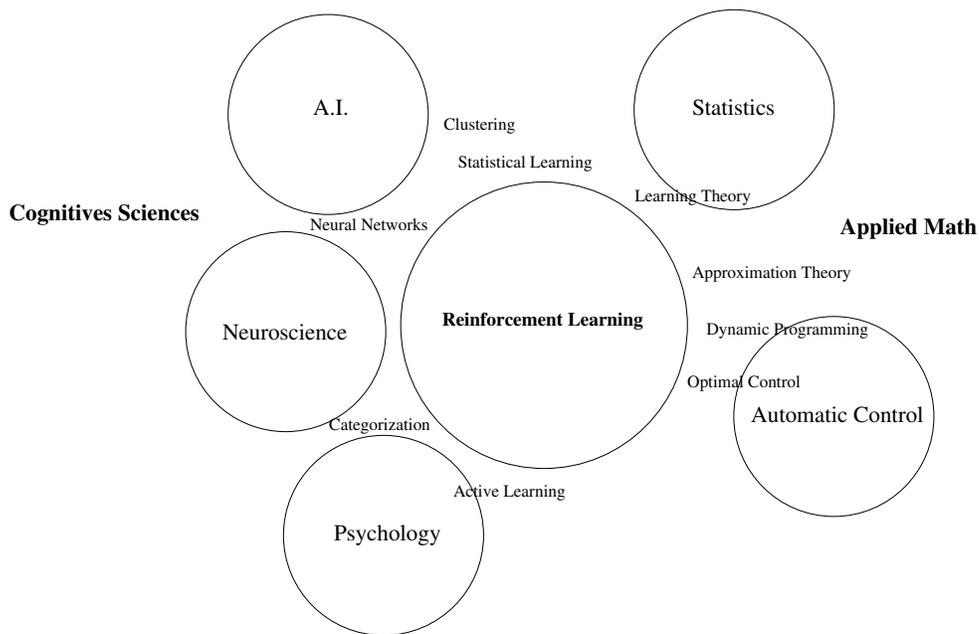
Reinforcement learning milestones

- “Programming a computer for playing chess” [Shannon, 1988].
- “Theory of Neural-Analog Reinforcement Systems” [Minsky, 1954].
- “Studies in machine learning using the game of checkers” [Samuel, 1959].
- “Trial and error” (tic-tac-toe player) [Michie, 1961].
- “BOXES: An experiment in adaptive control” (inverted pendulum) [Michie and Chambers, 1968].
- “Punish/Reward: Learning with a Critic in Adaptive Threshold Systems” (neural network) [Widrow et al., 1973].
- “Associative search network: A reinforcement learning associative memory” [Barto et al., 1981].
- “Temporal credit assignment in reinforcement learning” (temporal difference learning) [Sutton, 1984].
- “Learning from delayed rewards” (Q-learning) [Watkins, 1989].
- “Temporal difference learning and TD-Gammon” [Tesauro, 1995].

A machine learning paradigm

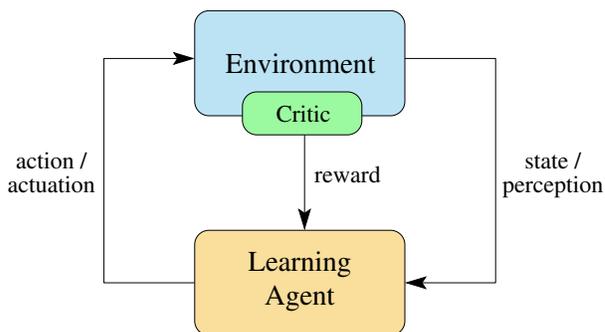
- *Supervised learning*: an expert (*supervisor*) provides examples of the right strategy (e.g., classification of clinical images). **Supervision is expensive.**
- *Unsupervised learning*: different objects are clustered together by similarity (e.g., clustering of images on the basis of their content). **No actual performance is optimized.**
- *Reinforcement learning*: learning by direct interaction (e.g., autonomous robotics). **Minimum level of supervision (reward) and maximization of long term performance.**

A multi-disciplinary field



2 The Reinforcement Learning Model

2.1 The Agent-Environment Interaction Protocol



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for  $t = 1, \dots, n$  do
  The agent perceives state  $s_t$ 
  The agent performs action  $a_t$ 
  The environment evolves to  $s_{t+1}$ 
  The agent receives reward  $r_t$ 
end for

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The environment: depending on how it reacts to the agent's actions and how it can be perceived by the agent, we have

- Fully controllable (e.g., chess), partially controllable (e.g., portfolio optimization)
- Deterministic (e.g., chess) or stochastic (e.g., backgammon)
- Adversarial (e.g., chess) or fixed (e.g., tetris)
- Fully observable (e.g., chess) or partially observable (e.g., robotics)
- Known (e.g., chess) or unknown (e.g., robotics)

The critic: it returns the **reinforcement**, which evaluates the quality of the action taken by the agent depending on its actual state.

The agent: defines the concept of *state* and *action* and it acts according to

- Open loop control
- Close loop control (i.e., *adaptive*)
- Non-stationary close loop control (i.e., *learning*)

2.2 The Learning Problem

Objective: find the close loop strategy which maximizes the long term (average) sum of rewards.

Agent-environment model: How do we formalize the rules defining the dynamics of the environment and its interaction with the agent? \Rightarrow Markov decision processes [**Lecture 2**].

The credit assignment problem: How do we assign rewards to actions? How do we learn to give up short term rewards to get long term rewards? \Rightarrow Value functions [**Lecture 2**].

The representation problem: How do we represent complex solutions? can we somehow approximate them? \Rightarrow Function approximation [**Lecture 5/6**].

Information collection: What is the most effective way to collect information about the environment and the rewards? \Rightarrow Exploration/exploitation dilemma [**Lecture 4**].

The learning process: How do we learn the optimal strategy?

- Known model \Rightarrow Dynamic programming [**Lecture 2**].
- Unknown model incremental \Rightarrow Temporal difference algorithms [**Lecture 3**].
- Unknown model batch \Rightarrow Approximate dynamic programming [**Lecture 5**].

3 Successful stories in Reinforcement Learning

- TD-Gammon [Tesauro, 1995]: best backgammon player.
- KnightCap [Baxter et al., 1998]: chess player with \simeq 2500 ELO.

- Robotics [Schaal and Atkeson, 1994]: jugglers, balancers, acrobats.
- Mobile robotics [Thrun et al., 1999]: robot guide at the Smithsonian museum.
- Elevators control system [Crites and Barto, 1996].
- Package routing [Littman and Boyan, 1993].
- Job-shop scheduling [Zhang and Dietterich, 1995].
- Production manufacturing control [Mahadevan and Theodorou, 1998]
- Computer poker [University of Alberta, 2006]: first computer poker player to beat professional players.
- Computer go: computer players constantly beat amateurs and approaching master players.

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