

# PRIVACY-PRESERVING DECENTRALIZED MACHINE LEARNING

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HeKA seminar, Inserm/Inria  
March 29, 2021

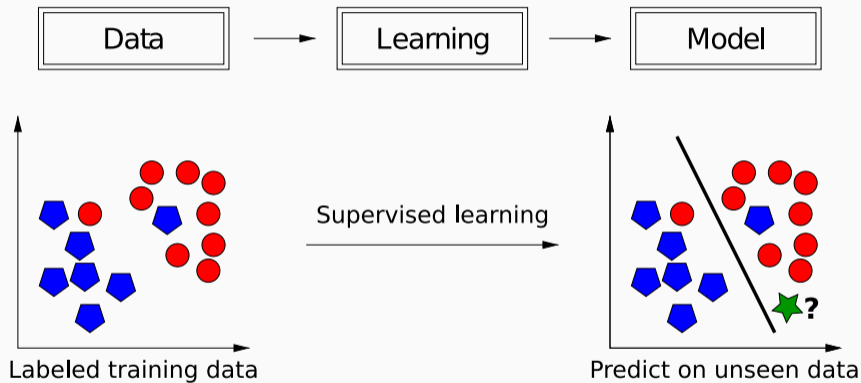
# OUTLINE OF THE TALK

1. Decentralized Machine Learning
2. Privacy in Decentralized Machine Learning
3. Applications to the medical domain
4. Wrapping up

# DECENTRALIZED MACHINE LEARNING

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# (SUPERVISED) MACHINE LEARNING





## A SHIFT OF PARADIGM: FROM CENTRALIZED TO DECENTRALIZED DATA

- The standard setting in Machine Learning (ML) considers a **centralized dataset processed in a tightly integrated system**
- But in the real world **data is often decentralized across many parties**





# WHY CAN'T WE JUST CENTRALIZE THE DATA?

## 1. Sending the data may be **too costly**

- Self-driving cars are expected to generate several TBs of data a day 
- Some wireless devices have limited bandwidth/power 

## 2. Data may be considered **too sensitive**

- We see a growing public awareness and regulations on data privacy   
(we could **try to anonymize the data**, but it is generally difficult to prevent all possible re-identification attacks without destroying utility)
- Keeping control of data can give a competitive advantage in business and research 

## HOW ABOUT EACH PARTY LEARNING ON ITS OWN?

1. The local dataset may be **too small**
  - Sub-par predictive performance (e.g., due to overfitting)
  - Non-statistically significant results (e.g., medical studies)
2. The local dataset may be **biased**
  - Not representative of the target distribution



## A BROAD DEFINITION OF DECENTRALIZED MACHINE LEARNING

- Decentralized Machine Learning (DML), also called Federated Learning, aims to collaboratively train a ML model while keeping the data decentralized

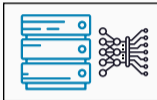




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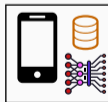
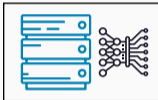
initialize model



## A BROAD DEFINITION OF DECENTRALIZED MACHINE LEARNING

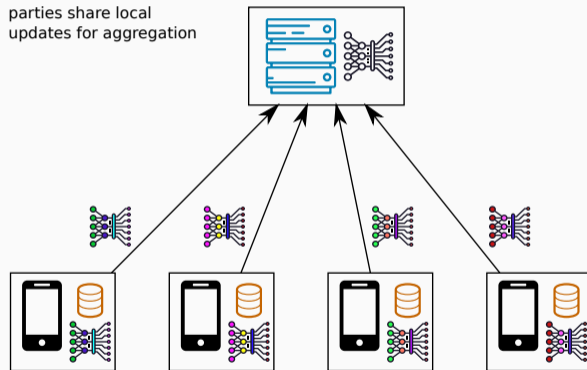
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each party makes an update  
using its local dataset



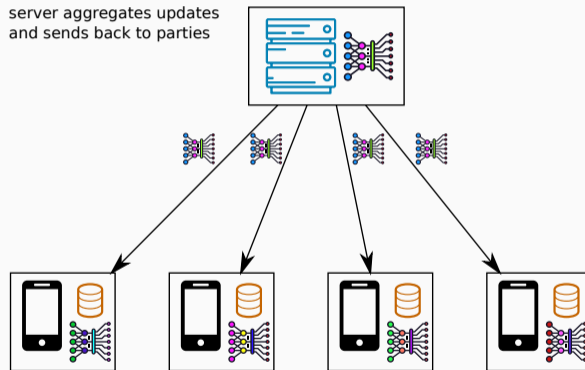
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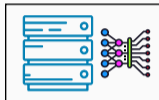
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## A BROAD DEFINITION OF DECENTRALIZED MACHINE LEARNING

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parties update their copy of the model and iterate



- We would like the final model to be as good as the centralized solution (ideally), or at least better than what each party can learn on its own

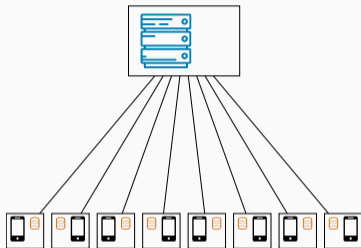
## Data distribution

- In distributed learning, **data is centrally stored** (e.g., in a data center)
  - The main goal is just to **train faster**
  - We control how data is distributed across workers: usually, it is **distributed uniformly at random** across workers
- In DML, **data is naturally distributed and generated locally**
  - Data is **not** independent and identically distributed (**non-i.i.d.**), and it is **imbalanced**

## Additional challenges that arise in DML

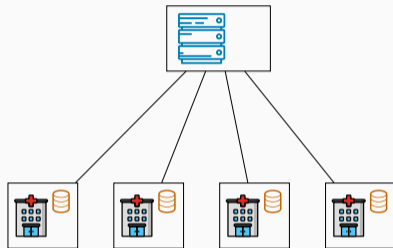
- Enforcing **privacy constraints**
- Dealing with the possibly **limited reliability/availability** of participants
- Achieving robustness against **malicious parties**
- ...

## Cross-device DML



- Massive number of parties (up to  $10^{10}$ )
- Small dataset per party (could be size 1)
- Limited availability and reliability
- Some parties may be malicious

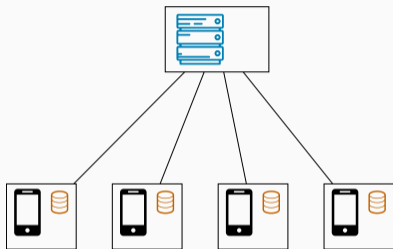
## Cross-silo DML



- 2-100 parties
- Medium to large dataset per party
- Reliable parties, almost always available
- Parties are typically honest

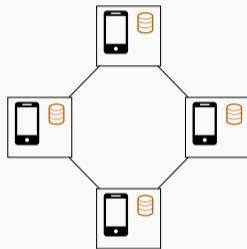
## SERVER ORCHESTRATED VS. FULLY DECENTRALIZED DML

### Server-orchestrated DML



- Server-client communication
- Global coordination, global aggregation
- Server is a single point of failure and may become a bottleneck

### Fully decentralized DML



- Direct communication between parties
- No global coordination, local aggregation
- Naturally scales to a large number of participants



- We consider a set of  $K$  parties (clients)
- Each party  $k$  holds a dataset  $\mathcal{D}_k$  of  $n_k$  points, so there is  $n = \sum_k n_k$  points in total
- We denote by  $\theta$  the model parameters (e.g., weights of a neural network)
- We want to find the parameters that minimize the overall prediction error:

$$\min_{\theta} \sum_{k=1}^K \frac{n_k}{n} \text{Loss}(\theta; \mathcal{D}_k)$$

- **Main idea:** clients update model with gradient descent to make it better on local data, server performs a weighted average of client updates

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## Algorithm FedAvg (server-side)

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initialize  $\theta$

**for** each round  $t = 0, 1, \dots$  **do**

**for** each client  $k$  in parallel **do**

$\theta_k \leftarrow \text{ClientUpdate}(k, \theta)$

$\theta \leftarrow \sum_{k=1}^K \frac{n_k}{n} \theta_k$

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## Algorithm ClientUpdate( $k, \theta$ )

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**Parameters:** number of local steps  $L$

    learning rate  $\eta$

**for** each local step  $1, \dots, L$  **do**

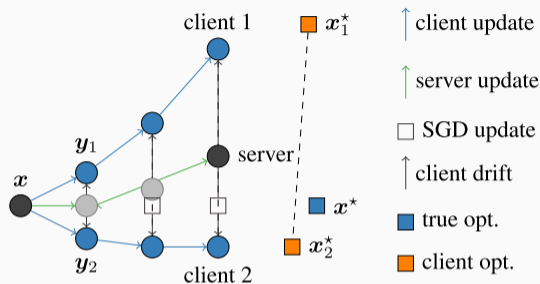
$\theta \leftarrow \theta - \eta \nabla \text{Loss}(\theta; \mathcal{D}_k)$

    send  $\theta$  to server

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- $L > 1$  allows to **reduce the number of communication rounds**
- Can be extended to the fully decentralized case [Lian et al., 2017, Koloskova et al., 2020]

## A KEY CHALLENGE: DEALING WITH HETEROGENEOUS DATA



(Figure taken from [Karimireddy et al., 2020])

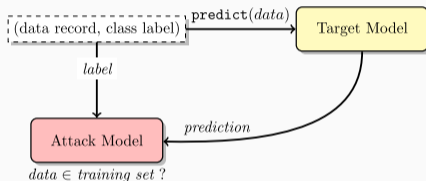
- When local datasets are non-i.i.d., FedAvg suffers from **client drift**
- Recent work on **correcting updates** [Karimireddy et al., 2020, Li et al., 2020]
- Can also **learn personalized models** [Smith et al., 2017, Zantedeschi et al., 2020]

# PRIVACY IN DECENTRALIZED MACHINE LEARNING

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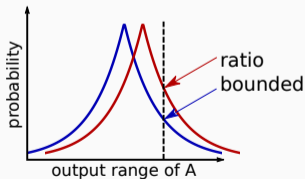
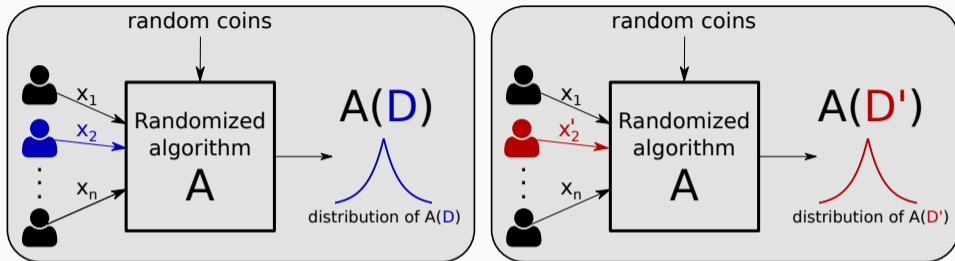
## PRIVACY ISSUES IN (DECENTRALIZED) ML

- ML models are susceptible to various attacks on data privacy
- **Membership inference attacks** try to infer the presence of a known individual in the training set, e.g., by exploiting the confidence in model predictions [Shokri et al., 2017]



- **Reconstruction attacks** try to infer some of the points used to train the model, e.g., by differencing attacks [Paige et al., 2020]
- **Decentralized ML offers an additional attack surface** because the server and/or other clients see intermediate model updates (not only the final model) [Nasr et al., 2019]

# DIFFERENTIAL PRIVACY IN A NUTSHELL



Definition ([Dwork et al., 2006], informal)

$\mathcal{A}$  is  $(\epsilon, \delta)$ -differentially private (DP) if for all neighboring datasets  $\mathcal{D} = \{x_1, x_2, \dots, x_n\}$  and  $\mathcal{D}' = \{x_1, x'_2, x_3, \dots, x_n\}$  and all possible sets of outputs  $S$ :

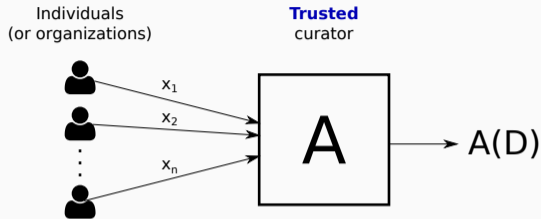
$$\Pr[\mathcal{A}(\mathcal{D}) \in S] \leq e^\epsilon \Pr[\mathcal{A}(\mathcal{D}') \in S] + \delta.$$

## KEY PROPERTIES OF DIFFERENTIAL PRIVACY

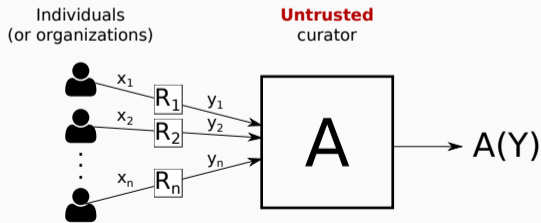
- DP is **immune to post-processing**: it is impossible to compute a function of the output of the private algorithm and make it less differentially private
- DP is **robust to arbitrary auxiliary knowledge** (worst-case model): the guarantee is just as strong if the adversary knows all but one record and regardless of the adversary strategy and computational power
- DP is **robust under composition**: if multiple analyses are performed on the same data, as long as each one satisfies DP, all the information released taken together will still satisfy DP (albeit with a degradation in the parameters)

## TWO SETTINGS: CENTRALIZED VS DECENTRALIZED

Centralized setting (also called global setting or trusted curator setting):  $\mathcal{A}$  is differentially private wrt dataset  $\mathcal{D}$



Decentralized/federated setting (also called local setting or untrusted curator setting): each  $\mathcal{R}_k$  is DP wrt record  $x_k$  (or local dataset  $\mathcal{D}_k$ )





- Most server-orchestrated DML algorithms follow the same high-level strategy:

**for**  $t = 1$  to  $T$  **do**

At each party  $k$ : compute  $\theta_k \leftarrow \text{LOCALUPDATE}(\theta, \theta_k)$ , send  $\theta_k$  to server

At server: compute  $\theta \leftarrow \frac{1}{K} \sum_k \theta_k$ , send  $\theta$  back to the participants

- Therefore:

DP aggregation + Composition property of DP  $\implies$  DP-DML

- **Differentially private aggregation:** given a private value  $x_k \in \mathbb{R}$  for each party  $k$ , we want to accurately estimate  $x^{\text{avg}} = \frac{1}{K} \sum_k x_k$  under an  $(\epsilon, \delta)$ -DP constraint

- **Centralized setting**: trusted curator adds (Gaussian) noise to the average  $x^{avg}$
- **Decentralized setting**: each party  $k$  adds noise to  $x_k$  before sharing it
- For a fixed DP guarantee, **the error is  $O(\sqrt{K})$  larger in the decentralized case!**
- Cryptographic primitives such as **secure aggregation** [Bonawitz et al., 2017] and **secure shuffling** [Balle et al., 2019] can be used to close this gap **but pose practical implementation challenges**

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**Algorithm** GOPA protocol

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**Parameters:** graph  $G$ , variances  $\sigma_{\Delta}^2, \sigma_{\eta}^2 \in \mathbb{R}^+$

for all neighboring parties  $\{k, l\}$  in  $G$  do

$k$  and  $l$  draw  $y \sim \mathcal{N}(0, \sigma_{\Delta}^2)$

set  $\Delta_{k,l} \leftarrow y, \Delta_{l,k} \leftarrow -y$

for each party  $k$  do

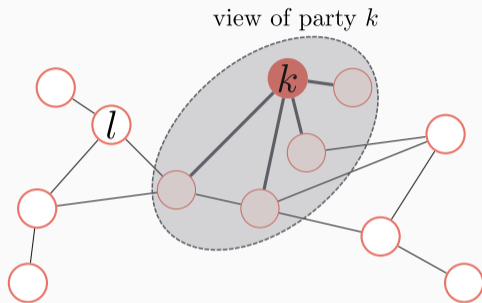
$k$  draws  $\eta_k \sim \mathcal{N}(0, \sigma_{\eta}^2)$

$k$  reveals  $\hat{x}_k \leftarrow x_k + \sum_{l \sim k} \Delta_{k,l} + \eta_k$

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1. Neighbors  $\{k, l\}$  in  $G$  securely exchange pairwise-canceling Gaussian noise
2. Each party  $k$  generates personal Gaussian noise
3. Party  $k$  reveals the sum of private value, pairwise and personal noise terms

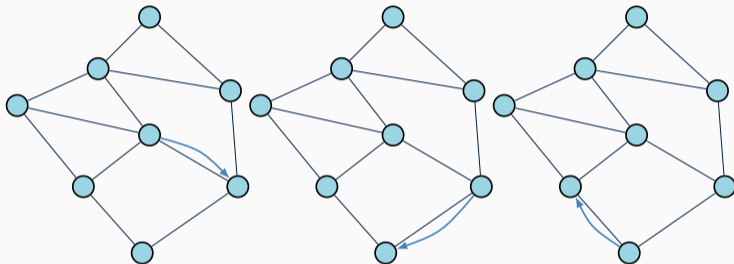
- **Accurate:** the result  $\hat{x}^{avg} = \frac{1}{K} \sum_k \hat{x}_k$  can match the accuracy of the centralized setting
- **Scalable:** it is sufficient for each party to communicate with  $O(\log K)$  others
- **Robust:** it can handle some collusions, dropouts and malicious behavior



- In the fully decentralized case, each party has a limited view of the system
- Can this be used to prove stronger differential privacy guarantees?

## PRIVACY BENEFITS OF FULL DECENTRALIZATION [CYFFERS AND BELLET, 2020]

- Consider algorithms that sequentially update the estimate (e.g., ML model) by following a **walk over the network graph** [Ram et al., 2009, Mao et al., 2020]



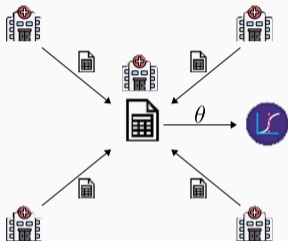
- We have shown that for some topologies (directed ring, complete graph), **such algorithms can match the privacy-utility trade-off of the centralized setting**
- Analysis relies on recent **privacy amplification** results [Balle et al., 2018] [Erlingsson et al., 2019, Feldman et al., 2018]

# APPLICATIONS TO THE MEDICAL DOMAIN

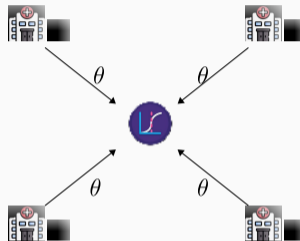
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# MULTI-CENTRIC MEDICAL STUDIES

Classic multi-centric study



Decentralized multi-centric study



- Multi-centric studies augment the statistical power of studies
- Decentralized studies could be **easier to set up**, could **minimize privacy risks**, and their results could be **updated more regularly**

- Development of a **decentralized machine learning library**
- **Proof of concept** across hospitals of the G4 alliance as short term objective
- **Identification of end-users needs** and appropriate workflow with clinicians
- **Understanding the regulatory requirements**, in relation with CNIL



## WRAPPING UP

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## CONCLUDING REMARKS

- Strong interest in ML community for decentralized/federated approaches, see recent survey [Kairouz et al., 2019]
- Can have differential privacy guarantees for these algorithms with the same utility as in the centralized setting:
  - via private aggregation, with a reasonable computational and communication overhead
  - via certain fully decentralized algorithms
- Compared to sharing “anonymized” data, DML restricts the usage to a specific ML analysis but can offer more robust privacy guarantees and/or better utility
- Clear applications to the medical domain

THANK YOU FOR YOUR ATTENTION!

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- **Adversary:** proportion  $1 - \rho$  of **colluding malicious parties** who observe all communications they take part in
- Denote by  $H$  the set of honest-but-curious parties, and by  $G^H$  the honest subgraph
- GOPA can achieve  $(\epsilon, \delta)$ -DP for any  $\epsilon, \delta > 0$  for **connected  $G^H$**  and **large enough  $\sigma_\eta^2, \sigma_\Delta^2$**
- We show that  **$\sigma_\eta^2$  can be as small as in the centralized setting** (matching its utility)
- We show that the required  $\sigma_\Delta^2$  depends on the **topology of  $G^H$**

### Theorem (Case of random $m$ -out graph)

Let  $\varepsilon, \delta' \in (0, 1)$  and let:

- $G$  be obtained by letting all parties randomly choose  $m = O(\log(\rho n)/\rho)$  neighbors
- $\sigma_\eta^2$  so as to satisfy  $(\varepsilon, \delta)$ -DP in the centralized (trusted curator) setting
- $\sigma_\Delta^2 = O(\sigma_\eta^2 |H|/m)$

Then GOPA is  $(\varepsilon, \delta)$ -differentially private for  $\delta = O(\delta')$ .

- Trusted curator utility with logarithmic number of messages per party
- Our theoretical results give practical values for  $m$  and  $\sigma_\Delta^2$

- **Utility can be compromised by malicious parties** tampering with the protocol (e.g., sending incorrect values to bias the outcome)
- It is impossible to force a party to give the “right” input (this also holds in the trusted curator setting)
- We enable each party  $u$  to **prove the following properties**:

$$\begin{array}{ll}
 x_k \in [0, 1], & \forall k \in \{1, \dots, K\} \\
 \Delta_{k,l} = -\Delta_{l,k}, & \forall \{k, l\} \text{ neighbors in } G \\
 \eta_k \sim \mathcal{N}(0, \sigma_\eta^2), & \forall k \in \{1, \dots, K\} \\
 \hat{x}_k = x_k + \sum_{l \sim k} \Delta_{k,l} + \eta_k, & \forall k \in \{1, \dots, K\}
 \end{array}$$

- Parties publish an encrypted log of the computation using **Pedersen commitments** [Blum, 1983, Pedersen, 1991], which are additively homomorphic
- Based on these commitments, parties prove that the computation was done correctly using **zero knowledge proofs**

### Theorem (Informal)

*A party  $k$  that passes the verification proves that  $\hat{x}_k$  was computed correctly. Additionally, by doing so,  $k$  does not reveal any additional information about  $x_k$ .*

- Costs per party remain linear in the number of neighbors
- Can **prove consistency across multiple runs** on same/similar data
- Can **handle drop out**

- Each party  $k$  holds a local dataset  $\mathcal{D}_k$ , joint dataset  $\mathcal{D} = \mathcal{D}_1 \cup \dots \cup \mathcal{D}_K$
- $\mathcal{D} \sim_k \mathcal{D}'$  means that datasets  $\mathcal{D}$  and  $\mathcal{D}'$  differ only on party  $k$ 's data
- $\mathcal{O}_k(\mathcal{A}(\mathcal{D}))$ : **view of party  $k$**  (local memory and messages received)

### Definition (Network differential Privacy)

An algorithm  $\mathcal{A}$  is  $(\epsilon, \delta)$ -network differentially private if for all pairs of parties  $(k, l)$  and for all datasets  $\mathcal{D} \sim_k \mathcal{D}'$ :

$$\Pr(\mathcal{O}_l(\mathcal{A}(\mathcal{D}))) \leq e^\epsilon \Pr(\mathcal{O}_l(\mathcal{A}(\mathcal{D}'))) + \delta.$$

## SIMPLE EXAMPLE: REAL SUMMATION ON A RING

- Each party  $k$  has  $M$  values  $x_k^1, \dots, x_k^M$  and we want to estimate  $\bar{x} = \sum_{k=1}^K \sum_{m=1}^M x_k^m$
- Let  $\text{Perturb}(\cdot; \sigma)$  satisfy  $(\epsilon, \delta)$ -local DP

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**Algorithm** Private real summation on a ring

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$\tau \leftarrow 0; a \leftarrow 0$

**for**  $m = 1$  to  $M$  **do**

**for**  $k = 1$  to  $K$  **do**

**if**  $a = 0$  **then**

$\tau \leftarrow \tau + \text{Perturb}(x_k^m; \sigma)$

$a = K - 2$

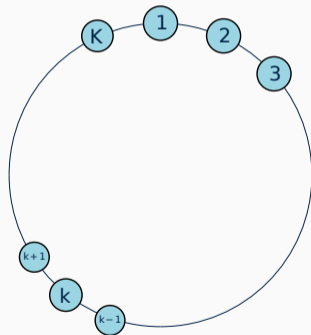
**else**

$\tau \leftarrow \tau + x_k^m$

$a \leftarrow a - 1$

**return**  $\tau$

---



### Theorem (Privacy-utility guarantee)

Let  $\epsilon, \delta > 0$ . The previously introduced algorithm

- outputs an unbiased estimate of  $\bar{x}$  with standard deviation  $\sqrt{\lceil MK/(K-1) \rceil} \sigma$ ,
- satisfies  $(\sqrt{2M \ln(1/\delta')} \epsilon + M\epsilon(e^\epsilon - 1), M\delta + \delta')$ -network DP for any  $\delta' > 0$ .

- Same privacy-utility trade-off as a **trusted aggregator**
- **Gain of  $O(1/\sqrt{K})$**  compared to local DP