

# CONTRIBUTIONS TO DECENTRALIZED AND PRIVACY-PRESERVING MACHINE LEARNING

HABILITATION THESIS (HDR) DEFENSE

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November 30, 2021



Design ML algorithms that  
take into account  
societal and ethical issues

## WHAT DRIVES MY RESEARCH

Design ML algorithms that  
**take into account**  
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**Make ML algorithms accessible to**  
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- **Decentralized ML:** learn collaboratively while keeping control of your data
- **Privacy-preserving ML:** ensure ML does not leak your sensitive data
- **Fair ML:** ensure ML model does not discriminate or is not overly biased
- **Speech privacy:** use voice interfaces without being personally identifiable
- **Transparent & reproducible ML**
- **Open source development**

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# WHAT IS DECENTRALIZED AND PRIVACY-PRESERVING MACHINE LEARNING?

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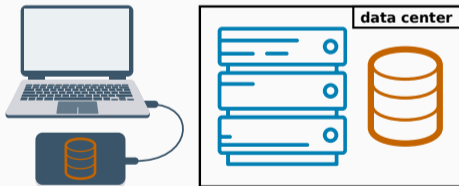
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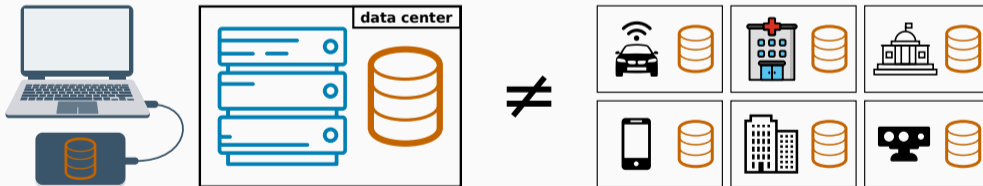
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## FROM CENTRALIZED TO DECENTRALIZED DATA

- The standard setting in ML considers a **centralized dataset** processed in a tightly integrated system
- But in the real world **data is often decentralized across many parties**



# WHY CAN'T WE JUST CENTRALIZE THE DATA?



## 1. Sending the data may be **too costly**

- Self-driving cars are expected to generate several TBs of data a day
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## 2. Data may be considered **too sensitive** to be shared

- We see a growing public awareness and regulations on data privacy 
- Keeping control of data can give a competitive advantage in business and research 

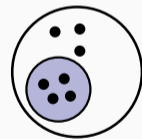
## HOW ABOUT EACH PARTY LEARNING ON ITS OWN?

1. The local dataset may be **too small**
  - Sub-par predictive performance (e.g., due to overfitting)
  - Non-statistically significant results (e.g., medical studies)



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2. The local dataset may be **biased**
  - Not representative of the target distribution



Decentralized learning (also called federated learning)

aims to collaboratively train ML models  
while keeping data decentralized

→ shared exploitation of the data rather than sharing the data itself

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- When I started working on this in 2015-2016, it was a newly emerging topic
- It is now in a booming phase<sup>1</sup>

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<sup>1</sup><https://www.forbes.com/sites/robtoews/2020/10/12/the-next-generation-of-artificial-intelligence/>

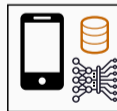
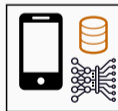
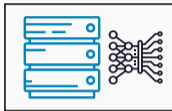
## DECENTRALIZED LEARNING: TYPICAL PROCESS





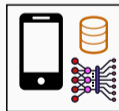
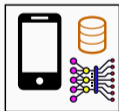
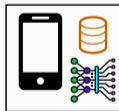
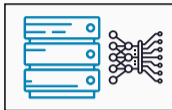
# DECENTRALIZED LEARNING: TYPICAL PROCESS

initialize model

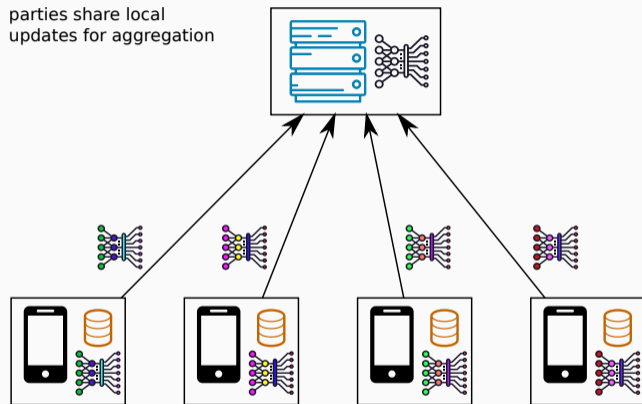


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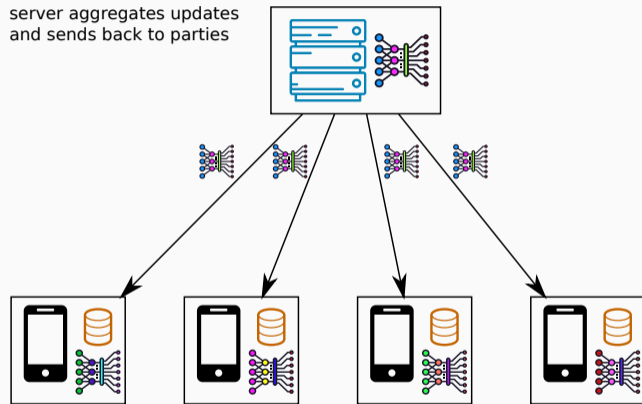
each party makes an update  
using its local dataset



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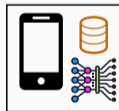
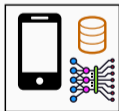
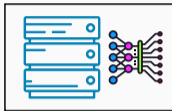


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parties update their copy  
of the model and iterate

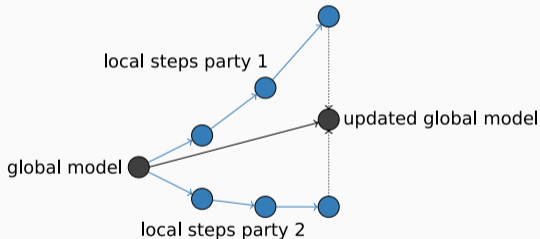


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- Decentralized learning comes with many challenges, distinct from those of classic distributed ML on a cluster (see our collaborative survey [[Kairouz et al., 2021](#)])

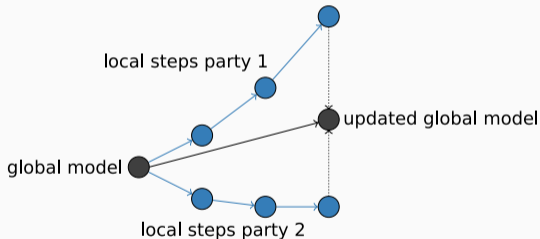
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- **Challenges:** design **low-communication** decentralized algorithms that **scale to many parties** and learn models that are **useful to all users**

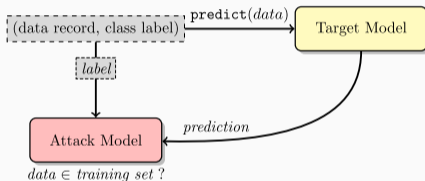


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- Not sharing data is insufficient to obtain robust privacy guarantees

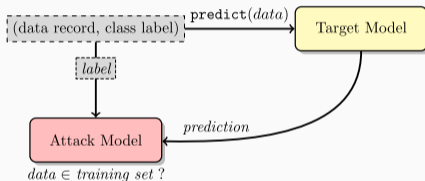
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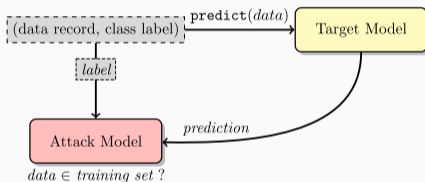
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- **Decentralized learning offers an additional attack surface** because the server and/or other parties observe model updates (not only the final model)
- **Challenges:** design decentralized learning algorithms with **rigorous privacy guarantees** while **minimizing the impact on the utility** of the resulting models

1. Decentralized Learning of **Personalized Models**
2. **Better Privacy-Utility Trade-offs** for Decentralized Learning

# DECENTRALIZED LEARNING OF PERSONALIZED MODELS

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## WARM-UP: LEARN A GLOBAL MODEL FOR EVERYONE

- A set of  $n$  users who behave honestly (i.e., follow the protocol)
- Each user  $u$  holds a dataset  $\mathcal{D}_u$  of  $m_u$  data points, and we let  $m = \sum_u m_u$
- Models with parameters  $\theta$  (e.g., weights of a linear classifier or neural network)
- A standard objective is to learn a global model by solving a problem of the form

$$\arg \min_{\theta} \sum_{u=1}^n \frac{m_u}{m} F_u(\theta; \mathcal{D}_u)$$

## PROPOSED FORMULATION: LEARN PERSONALIZED MODELS

- We propose to learn **personalized models**  $\Theta = (\theta_1, \dots, \theta_n)$  and a **similarity graph** represented by pairwise weights  $w = (w_{u,v})_{u < v}$  by solving

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- Captures flexible relationships: hyperparameter  $\lambda_1 \geq 0$  interpolates between learning **purely local models** and **a shared model per connected component**

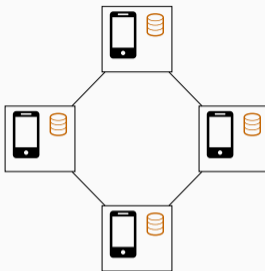
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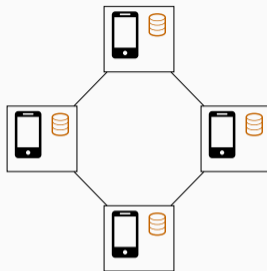
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- **Graph regularizer  $g(w)$** : avoid trivial graph, encourage sparsity

## FULLY DECENTRALIZED SETTING



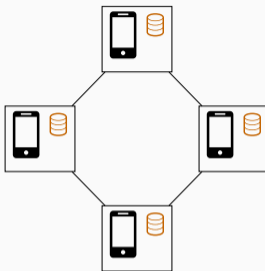
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- We **remove the need for a central server**: instead, **each user communicates with a small number of neighbors** in a network graph
- We consider an **asynchronous time model**: users become active asynchronously and in parallel at random times
  - **Naturally scales to many users** (as long as network graph is sparse)

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- At step  $t \geq 0$ , a random user  $u$  becomes active:
  1. user  $u$  combines a **weighted average of neighbors' models** and a **local gradient step**:

$$\theta_u(t+1) = (1 - \alpha)\theta_u(t) + \alpha \left( \sum_{v \in \mathcal{N}(u)} \frac{w_{u,v}}{d_u(w)} \theta_v(t) - \frac{m_u}{\lambda_1 m} \nabla F_u(\theta_u(t); \mathcal{D}_u) \right)$$

2. user  $u$  sends its updated model  $\theta_u(t+1)$  to its neighborhood  $\mathcal{N}(u)$

Reminder of the objective:  $\sum d_u(w) \frac{m_u}{m} F_u(\theta_u; \mathcal{D}_u) + \frac{\lambda_1}{2} \sum w_{u,v} \|\theta_u - \theta_v\|^2 + \lambda_2 g(w)$

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- At step  $t \geq 0$ , a random user  $u$  becomes active:
  1. Use peer sampling to contact a set  $\mathcal{V}$  of  $\rho$  users, request their model and degree
  2. Update the weights with users in  $\mathcal{V}$  via a gradient update
  3. Send each user  $v \in \mathcal{V}$  the updated weight  $w(t+1)_{u,v}$

Theorem (Convergence rates, informal [\[Bellet et al., 2018, Zantedeschi et al., 2020\]](#))

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1. For *fixed*  $w$ , let  $M(\Theta) = J(\Theta, w)$ . There exists  $\kappa > 0$  such that for any  $T > 0$ :

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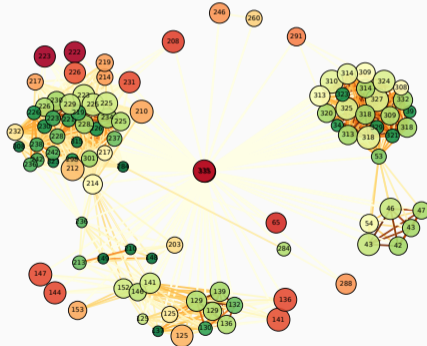
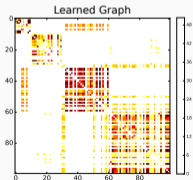
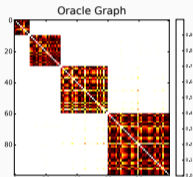
3. The alternating optimization of  $\Theta$  and  $w$  *converges to a local minimum of  $J$* .



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# EMPIRICAL RESULTS

- On heterogeneous data, our approach typically **outperforms both global and purely local models**
- Our formulation can **learn complex relationships between users**



We proposed to **learn personalized models** in a **fully decentralized setting**:

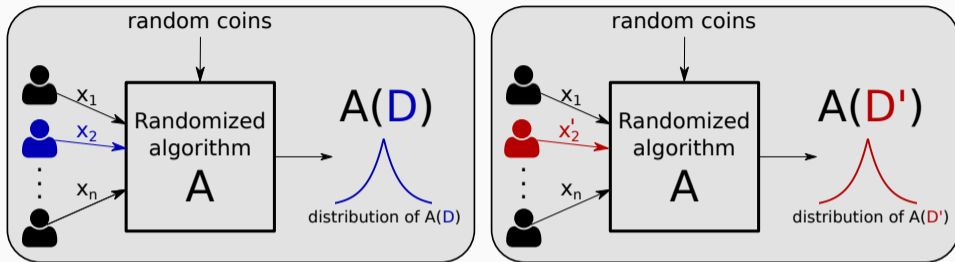
- We modeled **relationships between users** by a **sparse similarity graph**
- We leveraged this graph to **learn better personalized models for each user**
- We **jointly optimized the models and the graph**

→ the **first method for personalized decentralized learning**: this has become a standard approach to deal with heterogeneous data

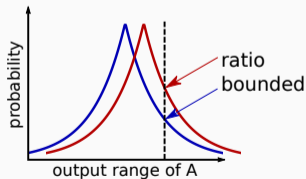
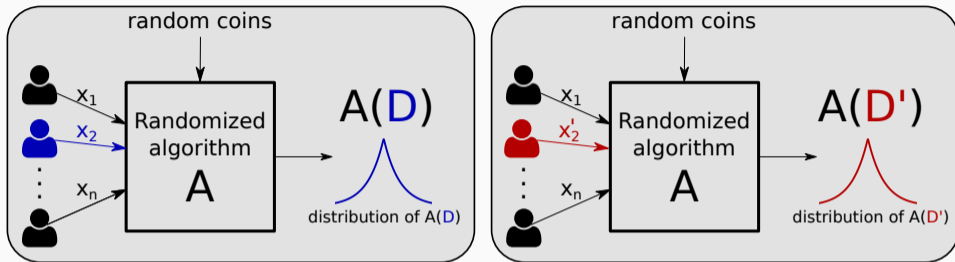
# BETTER PRIVACY-UTILITY TRADE-OFFS FOR DECENTRALIZED LEARNING

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# PRIVACY NOTION: DIFFERENTIAL PRIVACY



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Definition ([Dwork et al., 2006], informal)

$\mathcal{A}$  is  $(\epsilon, \delta)$ -DP if for all neighboring datasets  $\mathcal{D} = \{x_1, x_2, \dots, x_n\}$  and  $\mathcal{D}' = \{x_1, x'_2, x_3, \dots, x_n\}$  and all possible sets of outputs  $S$ :

$$\Pr[\mathcal{A}(\mathcal{D}) \in S] \leq e^\epsilon \Pr[\mathcal{A}(\mathcal{D}') \in S] + \delta.$$

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- Local DP is a suitable model for **decentralized learning without trusted parties** but, for a fixed  $(\epsilon, \delta)$ -DP guarantee, its **utility cost is typically  $\sqrt{n}$  larger**

- **Central DP:** a **trusted curator** collects raw data and runs a DP algorithm  $\mathcal{A}$  on it  $\rightarrow$  the output  $\mathcal{A}(\mathcal{D})$  is **only the final result**
  - **Local DP:** there is **no trusted curator** so each user must locally randomize its contributions  $\rightarrow$  the output  $\mathcal{A}(\mathcal{D})$  consists of **all messages sent by all users**
  - Local DP is a suitable model for **decentralized learning without trusted parties** but, for a fixed  $(\epsilon, \delta)$ -DP guarantee, its **utility cost is typically  $\sqrt{n}$  larger**
- $\rightarrow$  study **intermediate models** allowing better utility without relying on trusted parties

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- **Central DP:** trusted server computes  $\theta^{avg}$  and adds Gaussian noise
- **Local DP:** each user  $u$  adds (more) Gaussian noise to  $\theta_u$  before sharing it

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- **Estimate of the average:**  $\hat{\theta}^{avg} = \frac{1}{n} \sum_u \hat{\theta}_u = \theta^{avg} + \frac{1}{n} \sum_u \eta_u$

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- Set the independent noise variance so as to satisfy  $(\epsilon, \delta')$ -DP in the central model
- For large enough pairwise noise variance, GOPA is  $(\epsilon, \delta)$ -DP with  $\delta = O(\delta')$ .

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- Same utility as central DP with only logarithmic number of messages per user

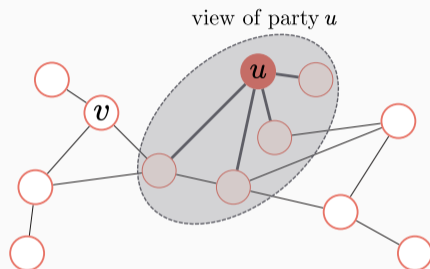
## HOW ABOUT FULLY DECENTRALIZED ALGORITHMS?

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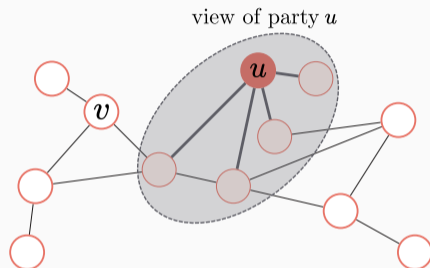
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## HOW ABOUT FULLY DECENTRALIZED ALGORITHMS?

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- But there is **no server observing all messages**, and each user  $u$  has a limited view
- **Question:** can this be used to **prove stronger differential privacy guarantees**?
- Motivated by previous work on private rumor spreading [Bellet et al., 2020]

- Let  $\mathcal{O}_u$  be the set of messages sent and received by user  $u$

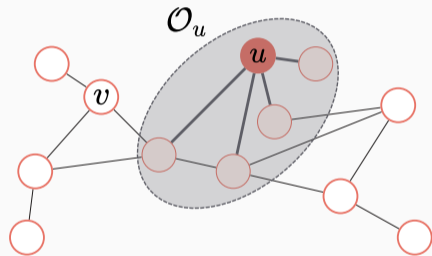
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## Definition (Network DP [Cyffers and Bellet, 2020])

An algorithm  $\mathcal{A}$  satisfies  $(\epsilon, \delta)$ -network DP if for all pairs of distinct users  $u, v \in \{1, \dots, n\}$  and all pairs of datasets  $\mathcal{D}, \mathcal{D}'$  that differ only in the local dataset of user  $v$ , we have:

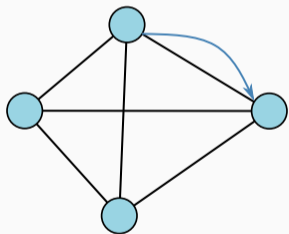
$$\Pr[\mathcal{O}_u(\mathcal{A}(\mathcal{D}))] \leq e^\epsilon \Pr[\mathcal{O}_u(\mathcal{A}(\mathcal{D}'))] + \delta.$$

- This is a relaxation of local DP: if  $\mathcal{O}_u$  contains the full transcript of messages, then network DP boils down to local DP



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- We consider a decentralized algorithm where the model is updated sequentially by following a random walk



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**Algorithm** Private decentralized SGD on a complete graph

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Initialize model  $\theta$

**for**  $t = 1$  to  $T$  **do**

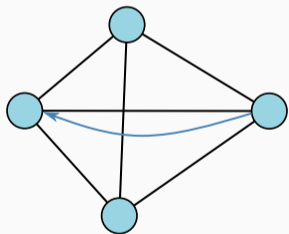
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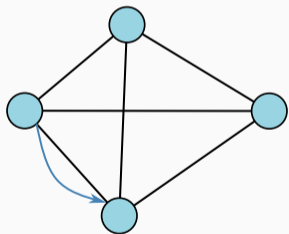
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- The proof leverages recent results on **privacy amplification by iteration** [Feldman et al., 2018] and exploits the randomness of the path taken by the model
- We show some **robustness to collusion** (albeit with smaller privacy amplification)

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→ **avoids costs and implementation issues of secure computation**-based solutions

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1. We designed a aggregation protocol for **decentralized learning with a server**  
→ **avoids costs and implementation issues of secure computation**-based solutions
2. We showed how to exploit the limited view of users in **fully decentralized algorithms**  
→ the first work to show that **full decentralization can amplify privacy guarantees**,  
providing a new motivation for such algorithms beyond scalability

# PUTTING DECENTRALIZED LEARNING TO PRACTICE

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## CHALLENGE 3: REAL DEPLOYMENTS

- **Technological challenges:** develop general-purpose software libraries which can be easily deployed in production systems
- **Regulatory/legal challenges:** when should model updates be considered as personal data? how to ensure compliance with current regulations (e.g., GDPR)?
- **Convincing stakeholders:** what are the key merits of decentralized learning for a given application? how to make it as transparent as possible to the end-users?

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- We have started **developing our own code base** and will soon deploy a **proof-of-concept across 4 French hospitals**
- Deployments on **concrete medical studies with real data** by the end of the year
- We have some **official support from CNIL** (the French Data Protection Authority) on legal aspects (such as writing DPIAs)<sup>2</sup>

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<sup>2</sup><https://www.cnil.fr/fr/bac-sable-donnees-personnelles-la-cnil-accompagne-12-projets-dans-le-domaine-de-la-sante-numerique>

FUTURE RESEARCH

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RELATED TOPICS

“Improve DP guarantees at no cost in utility by exploiting the way information is exchanged in fully decentralized ML”

(4-year grant funded by the French National Research Agency, started in 2021)

## Three complementary research directions:

1. (Broadening the scope of) privacy amplification by decentralization
2. Secure multi-party computation meets decentralized algorithms
3. Data-adaptive decentralized communication



Show that fully decentralized algorithms amplify privacy in a variety of settings

- General and time-evolving topologies to balance privacy, scalability and robustness
- Algorithms allowing more parallel computation
- Lower bounds on the error achievable under network DP
- Further relaxations, e.g. when each user may trust a few peers in the network

→ PhD of Edwige Cyffers

Combine secure multi-party computation (MPC) and decentralized algorithms

- Decentralized algorithms that use MPC primitives in local steps
- Trade-offs between computation, communication and privacy ruled by the number of parties involved in local steps
  - Postdoc (to hire) + collaborations with MPC experts like Adrià Gascón

Design data-adaptive topologies for faster convergence under heterogeneous data

- **Optimization of the topology** under statistical assumptions on data heterogeneity
- **General types of heterogeneity**, extending our work on label skew [Bellet et al., 2021]
- **Dynamic adaptation** of the topology while learning

→ Postdoc of **Batiste Le Bars** + collaboration with computing systems team at EPFL

An Inria-wide project on decentralized learning  
→ Coordinated by [G. Neglia](#) and myself, to start in 2022

- [Foster collaborations between Inria teams](#) on this topic
- [Multidisciplinary](#): ML, optimization, privacy & security, networks, systems...

## FUTURE RESEARCH

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BROADER TOPICS

- Achieving better privacy-utility trade-offs in private optimization may be possible by **making additional assumptions on the problem structure**
- We have recently started considering finer **coordinate-wise regularity** assumptions [Mangold et al., 2021]
- Assumptions about the **structure of the optimal solution** (such as sparsity) are promising directions to tackle high-dimensionality

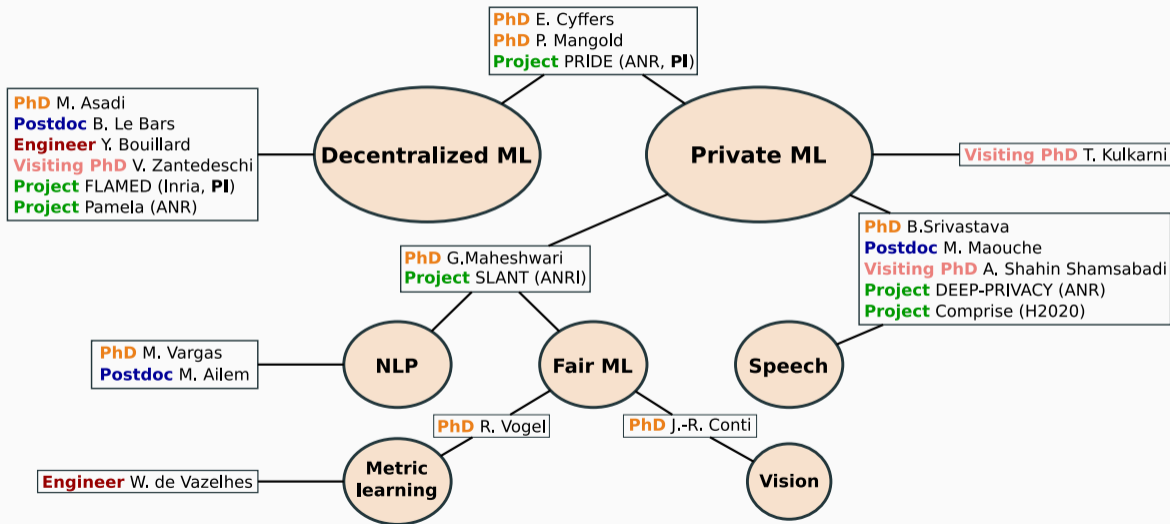
→ PhD of **Paul Mangold**

- Rich signals like **speech, images, and text** embed **various types of information**
- We typically want to **protect specific modalities** (e.g., personal attributes of the writer) while **fully retaining others** (e.g., the meaning of the text)
- **Formal notions like DP are necessary** to get clear guarantees, but need to be relaxed and combined with techniques from **representation learning and signal processing**
  - PhD of **Gaurav Maheshwari** (text), PhD of **Jean-Rémy Conti** (images)

THANK YOU FOR YOUR ATTENTION!



# SUMMARY OF PROJECTS AND SUPERVISION ACTIVITIES



- [Bellet et al., 2020] Bellet, A., Guerraoui, R., and Hendrikx, H. (2020).  
**Who started this rumor? Quantifying the natural differential privacy guarantees of gossip protocols.**  
In *DISC*.
- [Bellet et al., 2018] Bellet, A., Guerraoui, R., Taziki, M., and Tommasi, M. (2018).  
**Personalized and Private Peer-to-Peer Machine Learning.**  
In *AISTATS*.
- [Bellet et al., 2021] Bellet, A., Kermarrec, A.-M., and Lavoie, E. (2021).  
**D-Cliques: Compensating for Data Heterogeneity with Topology in Decentralized Federated Learning.**  
Technical report, arXiv:2104.07365.
- [Cyffers and Bellet, 2020] Cyffers, E. and Bellet, A. (2020).  
**Privacy Amplification by Decentralization.**  
Technical report, arXiv:2012.05326.
- [Dwork et al., 2006] Dwork, C., McSherry, F., Nissim, K., and Smith, A. (2006).  
**Calibrating noise to sensitivity in private data analysis.**  
In *Theory of Cryptography (TCC)*.

- [Feldman et al., 2018] Feldman, V., Mironov, I., Talwar, K., and Thakurta, A. (2018).  
**Privacy Amplification by Iteration.**  
In *FOCS*.
- [Jelasity et al., 2007] Jelasity, M., Voulgaris, S., Guerraoui, R., Kermarrec, A.-M., and van Steen, M. (2007).  
**Gossip-based peer sampling.**  
*ACM Trans. Comput. Syst.*, 25(3).
- [Kairouz et al., 2021] Kairouz, P., McMahan, H. B., Avent, B., Bellet, A., Bennis, M., Bhagoji, A. N., Bonawitz, K., Charles, Z., Cormode, G., Cummings, R., D’Oliveira, R. G. L., Eichner, H., Rouayheb, S. E., Evans, D., Gardner, J., Garrett, Z., Gascón, A., Ghazi, B., Gibbons, P. B., Gruteser, M., Harchaoui, Z., He, C., He, L., Huo, Z., Hutchinson, B., Hsu, J., Jaggi, M., Javidi, T., Joshi, G., Khodak, M., Konečný, J., Korolova, A., Koushanfar, F., Koyejo, S., Lepoint, T., Liu, Y., Mittal, P., Mohri, M., Nock, R., Özgür, A., Pagh, R., Qi, H., Ramage, D., Raskar, R., Raykova, M., Song, D., Song, W., Stich, S. U., Sun, Z., Suresh, A. T., Tramèr, F., Vepakomma, P., Wang, J., Xiong, L., Xu, Z., Yang, Q., Yu, F. X., Yu, H., and Zhao, S. (2021).  
**Advances and Open Problems in Federated Learning.**  
*Foundations and Trends® in Machine Learning*, 14(1–2):1–210.
- [Mangold et al., 2021] Mangold, P., Bellet, A., Salmon, J., and Tommasi, M. (2021).  
**Differentially Private Coordinate Descent for Composite Empirical Risk Minimization.**  
Technical report, arXiv:2110.11688.

- [Paige et al., 2020] Paige, B., Bell, J., Bellet, A., Gascón, A., and Ezer, D. (2020).  
**Reconstructing Genotypes in Private Genomic Databases from Genetic Risk Scores.**  
In *International Conference on Research in Computational Molecular Biology RECOMB*.
- [Sabater et al., 2020] Sabater, C., Bellet, A., and Ramon, J. (2020).  
**Distributed Differentially Private Averaging with Improved Utility and Robustness to Malicious Parties.**  
Technical report, arXiv:2006.07218.
- [Shokri et al., 2017] Shokri, R., Stronati, M., Song, C., and Shmatikov, V. (2017).  
**Membership Inference Attacks Against Machine Learning Models.**  
In *IEEE Symposium on Security and Privacy (S&P)*.
- [Zantedeschi et al., 2020] Zantedeschi, V., Bellet, A., and Tommasi, M. (2020).  
**Fully Decentralized Joint Learning of Personalized Models and Collaboration Graphs.**  
In *AISTATS*.